## Appendix I

We wish to relate the coefficients B, B<sub>1</sub>, in Eq. (IV-4) to A and A<sub>1</sub> in Eq. (IV-1). For small warping we may express the energy in the form

$$E = \frac{\pi^{2}k_{o}^{2}}{m^{*}} \left[ \frac{1}{2} (k/k_{o})^{2} + r (k/k_{o})^{4} Y_{4}(\theta, \phi) + s (k/k_{o})^{6} Y_{6}(\theta, \phi) \right]$$
 (A-1)

which is just Eq. (I-4) with s = rt.

Furthermore

$$\left(\frac{\partial E}{\partial k}\right)_{E_{\mathbf{F}}} = \frac{\hbar^{2}k_{o}}{\frac{*}{m}} \left[\left(\frac{k}{k_{o}}\right) + 4r\left(\frac{k}{k_{o}}\right)^{3} Y_{4}(\theta, \phi) + 6s\left(\frac{k}{k_{o}}\right)^{5} Y_{6}(\theta, \phi)\right] \quad (A-2)$$

where the derivative is evaluated at the Fermi energy.

Now we know that

$$(\frac{\partial E}{\partial k})_{E_F} (\frac{\partial k}{\partial E})_{E_F} = 1$$
 (A-3)

in any direction in k space. Equation (IV-4) gives  $(\frac{\partial k}{\partial E})_{E_F}$ .

We use the subscripts 1, 2, 3 to indicate the [100], [110], and [111] directions: the Kubic harmonics and  $(\frac{k}{k})$  are evaluated in these directions. For example

$$k_1 = (\frac{k}{k_0})_1 = (1 + A + A_1)$$
 (A-4)

using  $Y_4$ [100] =  $Y_6$ [100] = 1 in Eq. (IV-1).

Let us introduce the notation

$$\left[ \left( \frac{k}{k_0} \right)_i + 4r \left( \frac{k}{k_0} \right)_i^3 Y_4(i) + 6s \left( \frac{k}{k_0} \right)_i^5 Y_6(i) \right] = a_i (A, A_1, r, s) \quad (A-5)$$

where i runs from 1 to 3.

Substituting Eqs. (A-2), (A-5) and (IV-2) into Eq. (A-3) we obtain

$$(1 + B + B_1)\alpha_1 = (1 - \frac{B}{4} - \frac{13}{8}B_1)\alpha_2 = (1 - \frac{2B}{3} + \frac{16}{9}B_1)\alpha_3$$
 (A-6)

From this we obtain two linear equations for B and B<sub>1</sub> whose solution

$$B = \frac{\left| (\alpha_2 - \alpha_1) (\alpha_1 + \frac{13\alpha_2}{8}) \right|}{\left| (\alpha_3 - \alpha_1) (\alpha_1 - \frac{16\alpha_3}{9}) \right|}$$

$$\left| (\alpha_1 + \frac{\alpha_2}{4}) (\alpha_1 + \frac{13\alpha_2}{8}) \right|$$

$$\left| (\alpha_1 + \frac{2\alpha_3}{3}) (\alpha_1 - \frac{16\alpha_3}{9}) \right|$$

$$B_{1} = \frac{\left| (\alpha_{1} + \frac{\alpha_{2}}{4}) (\alpha_{2} - \alpha_{1}) \right|}{\left| (\alpha_{1} + \frac{2\alpha_{3}}{3}) (\alpha_{3} - \alpha_{1}) \right|}$$

$$\left| (\alpha_{1} + \frac{\alpha_{2}}{4}) (\alpha_{1} + \frac{13\alpha_{2}}{8}) \right|$$

$$\left| (\alpha_{1} + \frac{2\alpha_{3}}{3}) (\alpha_{1} - \frac{16\alpha_{3}}{9}) \right|$$

The a depend on r and s of Eq. (A-1); we now obtain these. We substitute

$$(\frac{k}{k_0}) = 1 + A Y_4 (0, \phi) + A_1 Y_6 (0, \phi) = k_i$$
 (IV-1)

into the expression for the energy, Eq. (A-1). The energy must be constant on the Fermi surface. By requiring the energy in the three principal directions to be the same, we obtain

$$1/2 k_1^2 + r k_1^4 + s k_1^6 = 1/2 k_2^2 - 1/4 r k_2^4 - \frac{13}{8} s k_2^6 =$$

$$1/2 k_3^2 - 2/3 r k_3^4 + \frac{16}{9} s k_3^6.$$
(A-7)